

# Gas permeability behavior of mullite-bonded porous silicon carbide ceramics

Shuqiang Ding · Yu-Ping Zeng · Dongliang Jiang

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**Abstract** An apparatus was developed to evaluate the gas permeability behavior of mullite ( $3\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$ )-bonded porous silicon carbide (SiC) ceramics at room temperature. The permeability was calculated according to Forchheimer's equation for the compressible gas. It was found that the sintering temperature and graphite (pore former) addition during the fabrication of the porous ceramics affect the permeability extremely by varying the texture of porous ceramics such as the open porosity, pore size distribution and tortuosity of pore channels. The increased sintering temperature results in a decreased Darcian (viscous) permeability but an increased non-Darcian (inertial) permeability. However, more graphite additions lead to the larger Darcian and non-Darcian permeability.

## Introduction

Porous silicon carbide (SiC) ceramics have been considered as one of the most favorite candidates for hot gas cleanup, melt metal filtration, catalytic substrate and thermal insulation, owing to their low bulk density, high permeability, high temperature stability, corrosion resistance and excellent catalytic activity [1–4]. Various processes, such as the particle stacking [5], pore former [6], template replication [7] and bubble generation [8], were developed to fabricate porous SiC ceramics. At the same time, the bulk density, open porosity, pore size distribution, strength,

coefficient of thermal expansion, thermal shock resistance, high temperature-oxidation resistance and acid/alkaline endurance of porous SiC ceramics were also studied in detailed [9–11]. In practical applications, the permeability of porous media need be quantified to investigate the efficiency of the hot gas filtration in the porous catalytic substrate, coal-gasification-generation process and diesel exhaust system. However, very limited information about the permeability of porous ceramics exists in the literature [12–16]. Particularly, there have been even less attention to the gas permeability behavior of porous SiC ceramics with the micrometric pore size [17].

In the present work, the gas permeability behavior of mullite ( $3\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$ )-bonded porous SiC ceramics with the pore size of 0.1–20  $\mu\text{m}$  and the open porosity of 25–62% was evaluated by a homemade permeability apparatus. Forchheimer's equation for the compressible gas was used to calculate the permeability. Effects of the sintering temperatures and graphite (pore former) additions during the fabrication on the permeability were investigated.

## Description of permeability

For laminary viscous flow through the porous material, Darcy's law, which establishes a linear dependence between the pressure gradient and the fluid velocity through the porous medium, is expressed for the incompressible fluid as [18–20]

$$\frac{P_i - P_o}{L} = \frac{\eta}{K_1} V_s, \quad (1)$$

where  $P_i$  is the fluid pressure at the entrance (Pa);  $P_o$  is the fluid pressure at the sample exit (Pa);  $L$  is the sample thickness (m);  $\eta$  is the viscosity of the fluid (Pa·s);  $K_1$  is the

S. Ding (✉) · Y.-P. Zeng · D. Jiang  
Shanghai Institute of Ceramics, Chinese Academy of Sciences,  
1295 Dingxi Road, Shanghai 200050, China  
e-mail: sqding@mail.sic.ac.cn

Darcian or viscous permeability ( $m^2$ );  $V_s$  is the fluid velocity (m/s), given by the volumetric flow rate divided by the sample cross-sectional area. Darcian permeability of porous media is the intrinsic property of porous media, independent of the fluid. When the compressibility of the fluid is considered, Eq. 1 is modified as follows

$$\frac{P_i^2 - P_o^2}{2PL} = \frac{\eta}{K_1} V_s, \quad (2)$$

where  $P$  is the fluid pressure at which  $V_s$  is measured.

Darcy's law considers only the viscous effects on the fluid pressure drop at very low flowing velocity. However, fluid flow through porous media usually deviates from Darcy's law with the increase of fluid velocity due to the contribution of inertia and turbulence. Forchheimer's equation, yielding more realistic and reliable permeability constants, has been proposed for the incompressible fluid as [21–23]

$$\frac{P_i - P_o}{L} = \frac{\eta}{K_1} V_s + \frac{\rho}{K_2} V_s^2, \quad (3)$$

where  $K_2$  is the non-Darcian or inertial permeability (m). The first term ( $\eta V_s/K_1$ ) represents viscous energy losses and prevails at low fluid velocity, while the second term ( $\rho V_s^2/K_2$ ) represents inertia energy losses and is more significant at high fluid velocity. When the compressibility of the fluid is considered, Eq. 3 is modified as follows

$$\frac{P_i^2 - P_o^2}{2PL} = \frac{\eta}{K_1} V_s + \frac{\rho}{K_2} V_s^2. \quad (4)$$

Considering the contribution of the inertia energy losses and gas compressibility as well as the viscous energy losses, Forchheimer's equation for the compressible gas is best model to evaluate the permeability of porous media [20, 23]. Therefore, Eq. 4 was adopted to calculate the permeability of porous SiC ceramics in this work.

## Experimental

Mullite-bonded porous SiC ceramics were fabricated by an in-situ reaction bonding process, described elsewhere [6, 24]. Briefly, the powder mixture of  $\alpha$ -SiC,  $Al_2O_3$  and graphite powder was compacted and subsequently sintered at 1,350–1,500 °C for 4 h in air. Graphite is burned out to produce pores and the surface of SiC is oxidized to  $SiO_2$  at high temperature. With further increasing the temperature, the amorphous  $SiO_2$  converts into cristobalite and reacts with  $\alpha$ - $Al_2O_3$  to form mullite. SiC particles are bonded by mullite and the oxidation-derived  $SiO_2$  to obtain porous

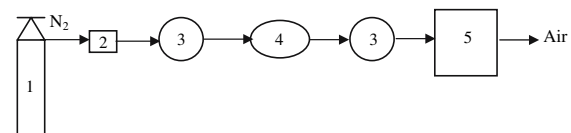
**Table 1** Characterization of the samples adopted in this work

Sample	SiC:Al <sub>2</sub> O <sub>3</sub> in green bodies (by volume)	Graphite content in green bodies (vol.%)	Sintering temperature (°C)
S1	3.65	0	1,450
S2	3.65	14.0	1,450
S3	3.65	27.2	1,450
S4	3.65	39.3	1,450
S5	3.65	39.3	1,350
S6	3.65	39.3	1,400
S7	3.65	39.3	1,500

SiC ceramics. Table 1 show the characterization of the samples adopted in this work.

The specimens were machined as the disks of 20.0 mm in diameter and 3.0 mm in thickness for the permeability measurement. Experimental evaluation of  $N_2$  permeability was conducted at room temperature (25 °C; for  $N_2$ ,  $\eta = 1.78 \times 10^{-5}$  Pa·s and  $\rho = 1.16$  kg/m<sup>3</sup>) by a homemade permeability apparatus. Figure 1 shows the schematic diagram of the permeability apparatus. Nitrogen gas was supplied by the  $N_2$  supply (1) and the output pressure was adjusted by pressure valve (2). The tested samples were fixed in the sample holder (4) between two chambers, leaving a circular gas-passing area. Subsequently, an inlet  $N_2$  pressure ( $P_i$ ) was applied to the samples and the volumetric  $N_2$ -flow rate ( $Q$ ) was measured under steady-state conditions at ambient pressure (0.1 MPa) by gas flow meter (5). The inlet pressure and the outlet pressure ( $P_o$ ) were measured by gas manometer (3). The volumetric  $N_2$ -flow rate ( $Q$ ) was converted to  $N_2$  velocity ( $V_s$ ) using the expression  $V_s = 4Q/\pi D^2$ , where  $D = 15.0$  mm is the sample diameter. Experimental data were fitted to Eq. 4 to obtain the permeability constant  $K_1$  and  $K_2$ .

Microstructure of mullite-bonded porous SiC ceramics was observed by scanning electron microscopy (SEM) (Model JSM-5600LV, JEOL, Japan). Pore size distribution was characterized by the mercury porosimetry (Model PoreSizer 9320, Micromeritics, USA). Open porosity was determined by the Archimedes method, where the distilled water was used as the liquid medium.



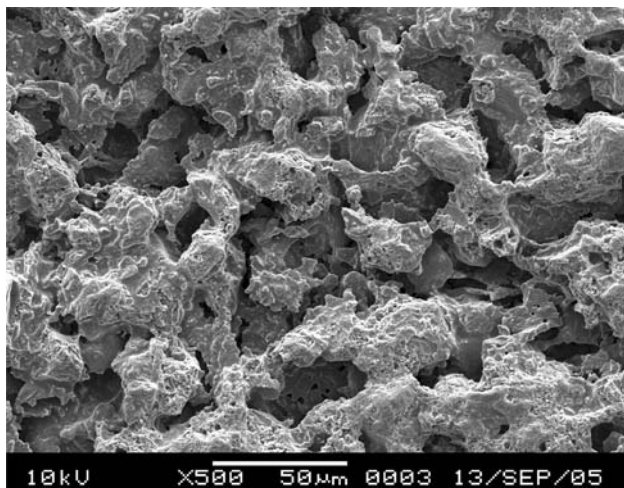
1- $N_2$  supply, 2-Pressure valve, 3-Gas manometer, 4-Sample holder, 5-Gas flow meter

**Fig. 1** Schematic diagram of permeability apparatus developed in this work

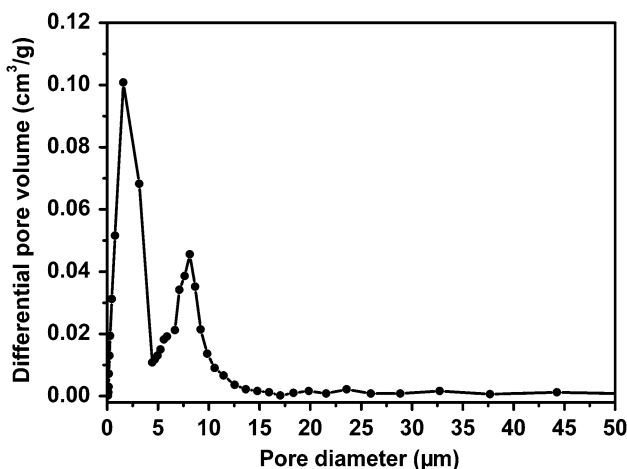
**Results and discussion**

Figure 2 shows the typical microstructure of as-fabricated porous SiC ceramics (sample S2). The stable structure with obviously connected pores was observed. A large number of pores exist among SiC particles and the pore size ranges from submicron to 20 μm. Figure 3 shows the further pore size distribution of the sample (sample S2). It takes on a narrow and bimodal pore size distribution at 1.6 and 8.0 μm, indicating that the texture of porous SiC ceramics is dominated by these two kinds of pores.

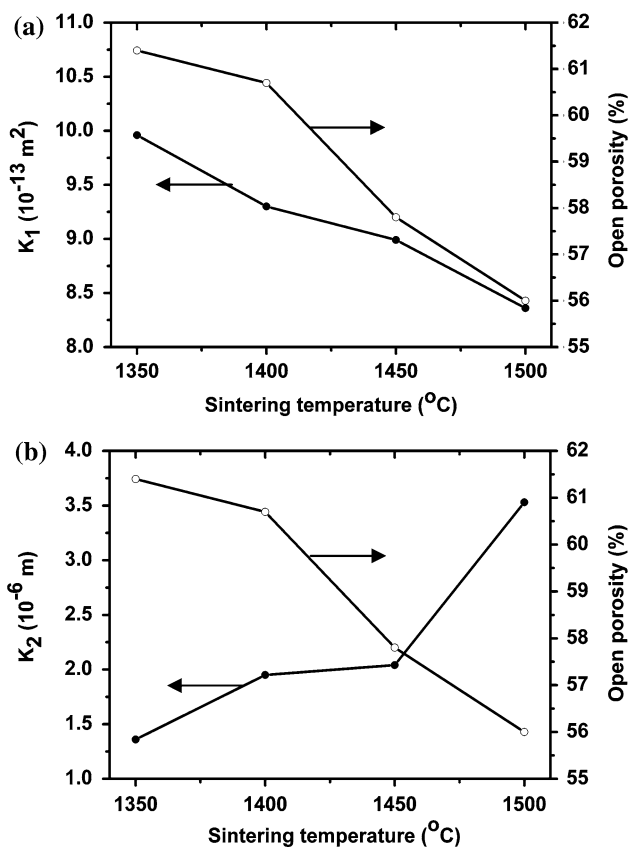
Figure 4 shows the open porosity and permeability of samples sintered at different temperatures for 4 h. For all the samples adopted, Darcian permeability  $K_1$  is in the same order of magnitude of  $10^{-13} \text{ m}^2$  while non-Darcian permeability  $K_2$  is in the order of magnitude of  $10^{-6} \text{ m}$ . The



**Fig. 2** SEM micrograph of mullite-bonded porous SiC ceramics (sample S2)



**Fig. 3** Pore size distribution of mullite-bonded porous SiC ceramics (sample S2)



**Fig. 4** Open porosity, (a) Darcian permeability  $K_1$  and (b) non-Darcian permeability  $K_2$  of samples sintered at different temperatures

increased sintering temperatures lead to a gradual decrease in open porosity and Darcian permeability, but a slight increase in non-Darcian permeability. Higher sintering temperatures result in more oxidation-derived  $\text{SiO}_2$  with low viscosity which accelerates the formation of mullite by viscous flowing. Acute viscous flow promotes the closure of small pores and the shrinkage of large pores, leading to the decrease in open porosity and pore size. At the same time, viscous flowing effect of  $\text{SiO}_2$  impairs the connectivity of open pores and then enlarges the tortuosity of pore channels.

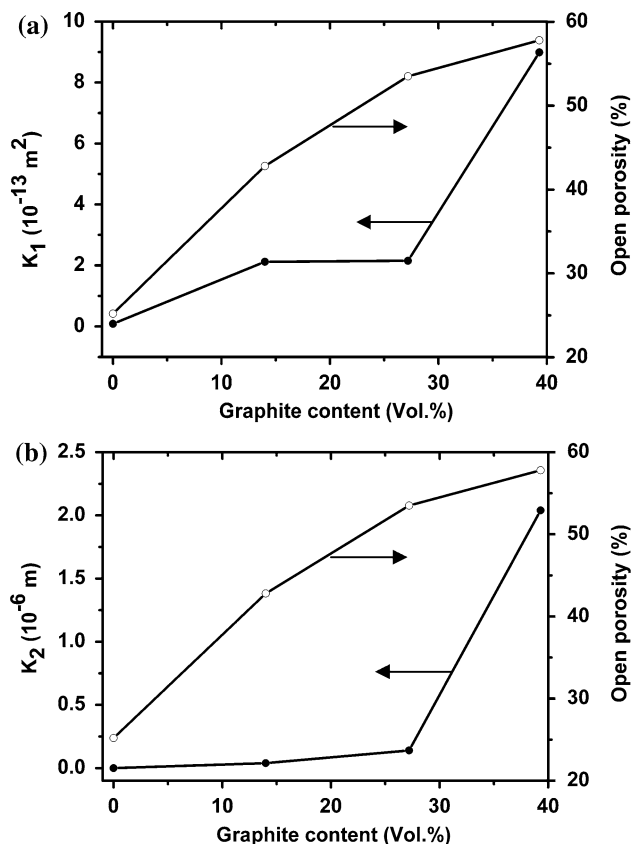
According to Carman–Kozeny’s relation [18]:

$$K_1 = \frac{pd^2}{16f_{CK}\tau^2}, \tag{5}$$

where  $K_1$  is Darcian permeability;  $p$  is the efficient porosity contributing to the permeability;  $d$  is the average pore diameter;  $f_{CK}$  is Carman–Kozeny coefficient; and  $\tau$  is the tortuosity of pore channels defined by the ratio between the mean length actually traveled by the fluid passing through the porous medium and the thickness of the porous medium in the macroscopic direction of the flow, Darcian permeability is in direct proportion to the efficient porosity and the

square of the average pore diameter but in inverse proportion to the square of the tortuosity. Efficient porosity is mainly contributed by the interconnected open pores going from one side to another of the porous sample. For high porous materials, the efficient porosity approaches the open porosity. Therefore, the decrease in the open porosity and pore diameter and the increase in the tortuosity reduce the Darcian permeability as sintering temperatures rise. With increasing the sintering temperatures, the dead-end porosity increases and more tortuous flow paths are generated. Then, the inertia interaction between gas and porous walls is enhanced even though the open porosity and pore diameter decrease slightly, resulting in the increase of inertia energy losses of flowing gas. Thus, the non-Darcian or inertial permeability increases with the sintering temperatures.

Figure 5 shows the open porosity and permeability of samples with different graphite additions in green bodies. The open porosity, Darcian permeability  $K_1$  and non-Darcian permeability  $K_2$  of porous SiC ceramics increase to a great extent as the graphite content in green bodies increases. Porous SiC ceramics with 14.0 vol.% graphite addition possess 1.7 times open porosity, 23.8 times  $K_1$  and 1857.1 times  $K_2$  of porous SiC ceramics without graphite content.



**Fig. 5** Open porosity, (a) Darcian permeability  $K_1$  and (b) non-Darcian permeability  $K_2$  as a function of graphite additions

In porous SiC ceramics, there are mainly two kinds of pores which correspond to two peaks in the curve of pore size distribution, as shown in Fig. 3. Small pores with  $\sim 1.6 \mu\text{m}$  derive from the stack of SiC particles while large pores with  $\sim 8.3 \mu\text{m}$  are formed by burning out graphite particles [24]. More graphite additions in green bodies increase the number of the large pores, resulting in the higher open porosity. The high porosity improves the connectivity of open pores and then reduces the tortuosity of pore channels. Furthermore, plenty of large pores by burning out graphite particles enlarge the average pore diameter in porous SiC ceramics. According to Eq. 5, the higher open porosity, larger average pore diameter and lower tortuosity lead to the larger Darcian permeability. Therefore, Darcian permeability of porous SiC ceramics increases with the graphite content. Due to the abrupt increase of the open porosity and pore size caused by the addition of graphite, more pore walls were formed. Then, the interaction between the flowing gas and pore walls is enhanced. The texture—non-Darcian permeability  $K_2$  relation of porous ceramics can be well-described by the following equation [21]

$$K_2 = \frac{ap^3d}{1-p}, \quad (6)$$

where  $a$  is the empirical constant depending on the pore shape and the tortuosity. Consequently, the addition of graphite improves the non-Darcian permeability by enlarging the open porosity and pore size.

## Conclusions

The  $\text{N}_2$  permeability behavior of mullite-bonded porous SiC ceramics with the open porosity of 25–62% and the bimodal pore size distribution between submicron and  $20 \mu\text{m}$  was investigated at room temperature. The results show that Darcian permeability is in the order of magnitude of  $10^{-13} \text{ m}^2$  while non-Darcian permeability  $K_2$  is in the order of magnitude of  $10^{-6} \text{ m}$ . With the increase of sintering temperatures, Darcian permeability of samples decreases because of the lower open porosity and smaller pore size. In addition, higher sintering temperatures generate more tortuous flow paths in porous ceramics which enhance the inertia interaction between the flowing gas and the pore walls, resulting in the higher non-Darcian permeability. However, the addition of graphite improves the Darcian and non-Darcian permeability by enlarging the open porosity and pore size.

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